

PART I : CHEMISTRY

SECTION - I

Single Correct Choice Type

This section contains 8 multiple choice questions. Each question has 4 choices (A), (B), (C) and (D) for its answer, out of which **ONLY ONE** is correct.

1. Given that the abundances of isotopes ^{54}Fe , ^{56}Fe and ^{57}Fe are 5%, 90% and 5%, respectively, the atomic mass of Fe is

(A) 55.85 (B) 55.95 (C) 55.75 (D) 56.05

Answer

☐ (A) ☒ (B) ☐ (C) ☐ (D)

2. The term that corrects for the attractive forces present in a real gas in the van der Waals equation is

(A) nb (B) $\frac{an^2}{V^2}$ (C) $-\frac{an^2}{V^2}$ (D) $-nb$

Answer

☐ (A) ☒ (B) ☐ (C) ☐ (D)

3. Among the electrolytes Na_2SO_4 , CaCl_2 , $\text{Al}_2(\text{SO}_4)_3$ and NH_4Cl , the most effective coagulating agent for Sb_2S_3 sol is

(A) Na_2SO_4 (B) CaCl_2 (C) $\text{Al}_2(\text{SO}_4)_3$ (D) NH_4Cl

Answer

☐ (A) ☐ (B) ☒ (C) ☐ (D)

4. The Henry's law constant for the solubility of N_2 gas in water at 298 K is 1.0×10^5 atm. The mole fraction of N_2 in air is 0.8. The number of moles of N_2 from air dissolved in 10 moles of water at 298 K and 5 atm pressure is

(A) 4.0×10^{-4} (B) 4.0×10^{-5} (C) 5.0×10^{-4} (D) 4.0×10^{-6}

Answer

☒ (A) ☐ (B) ☐ (C) ☐ (D)

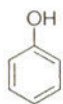
5. The reaction of P_4 with **X** leads selectively to P_4O_6 . The **X** is

(A) Dry O_2 (B) A mixture of O_2 and N_2
(C) Moist O_2 (D) O_2 in the presence of aqueous NaOH

Answer

☐ (A) ☒ (B) ☐ (C) ☐ (D)

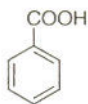
6. The correct acidity order of the following is



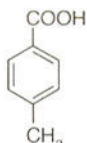
(I)



(II)



(III)



(IV)

- (A) (III) > (IV) > (II) > (I) (B) (IV) > (III) > (I) > (II)
(C) (III) > (II) > (I) > (IV) (D) (II) > (III) > (IV) > (I)

Answer

- ☒ (A) ☐ (B) ☐ (C) ☐ (D)

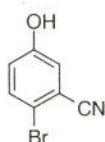
7. Among cellulose, poly(vinyl chloride), nylon and natural rubber, the polymer in which the intermolecular force of attraction is weakest is

- (A) Nylon (B) Poly(vinyl chloride)
(C) Cellulose (D) Natural Rubber

Answer

- ☐ (A) ☐ (B) ☐ (C) ☒ (D)

8. The IUPAC name of the following compound is



- (A) 4-Bromo-3-cyanophenol
(B) 2-Bromo-5-hydroxybenzonitrile
(C) 2-Cyano-4-hydroxybromobenzene
(D) 6-Bromo-3-hydroxybenzonitrile

Answer

- ☐ (A) ☒ (B) ☐ (C) ☐ (D)

SECTION – II

Multiple Correct Choice Type

This section contains 4 multiple choice questions. Each question has 4 choices (A), (B), (C) and (D) for its answer, out of which **ONE OR MORE** is/are correct.

9. The correct statement(s) regarding defects in solids is(are)

- (A) Frenkel defect is usually favoured by a very small difference in the sizes of cation and anion
(B) Frenkel defect is a dislocation defect
(C) Trapping of an electron in the lattice leads to the formation of F-center
(D) Schottky defects have no effect on the physical properties of solids

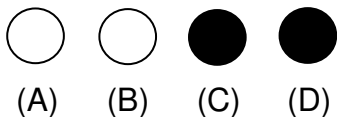
Answer

- ☐ (A) ☒ (B) ☒ (C) ☐ (D) **OR** ☐ (A) ☐ (B) ☒ (C) ☐ (D)

10. The compound(s) that exhibit(s) geometrical isomerism is(are)

- (A) $[\text{Pt}(\text{en})\text{Cl}_2]$ (B) $[\text{Pt}(\text{en})_2]\text{Cl}_2$
 (C) $[\text{Pt}(\text{en})_2\text{Cl}_2]\text{Cl}_2$ (D) $[\text{Pt}(\text{NH}_3)_2\text{Cl}_2]$

Answer



11. The compound(s) formed upon combustion of sodium metal in excess air is(are)

- (A) Na_2O_2 (B) Na_2O (C) NaO_2 (D) NaOH

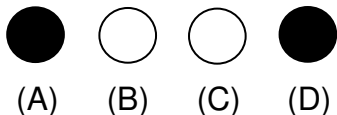
Answer



12. The correct statement(s) about the compound $\text{H}_3\text{C}(\text{HO})\text{HC}-\text{CH}=\text{CH}-\text{CH}(\text{OH})\text{CH}_3$ (**X**) is(are)

- (A) The total number of stereoisomers possible for **X** is 6
 (B) The total number of diastereomers possible for **X** is 3
 (C) If the stereochemistry about the double bond in **X** is *trans*, the number of enantiomers possible for **X** is 4
 (D) If the stereochemistry about the double bond in **X** is *cis*, the number of enantiomers possible for **X** is 2

Answer



SECTION - III

Comprehension Type

This section contains 2 groups of questions. Each group has 3 multiple choice questions based on a paragraph. Each question has 4 choices (A), (B), (C) and (D) for its answer, out of which **ONLY ONE** is correct.

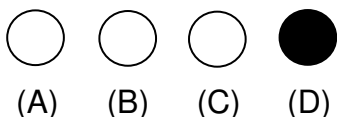
Paragraph for Question Nos. 13 to 15

p-Amino-*N,N*-dimethylaniline is added to a strongly acidic solution of **X**. The resulting solution is treated with a few drops of aqueous solution of **Y** to yield blue coloration due to the formation of methylene blue. Treatment of the aqueous solution of **Y** with the reagent potassium hexacyanoferrate(II) leads to the formation of an intense blue precipitate. The precipitate dissolves on excess addition of the reagent. Similarly, treatment of the solution of **Y** with the solution of potassium hexacyanoferrate(III) leads to a brown coloration due to the formation of **Z**.

13. The compound **X** is

- (A) NaNO_3 (B) NaCl (C) Na_2SO_4 (D) Na_2S

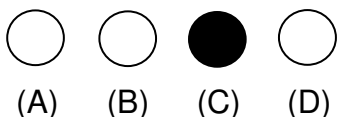
Answer



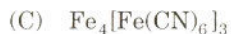
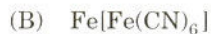
14. The compound **Y** is

- (A) MgCl_2 (B) FeCl_2 (C) FeCl_3 (D) ZnCl_2

Answer



15. The compound **Z** is



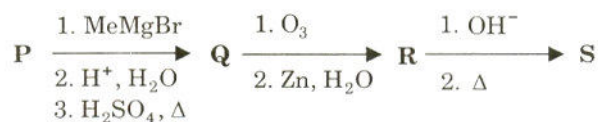
Answer



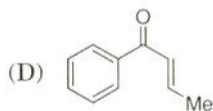
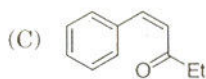
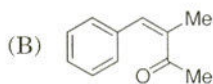
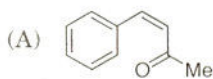
(A) (B) (C) (D)

Paragraph for Question Nos. 16 to 18

A carbonyl compound **P**, which gives positive iodoform test, undergoes reaction with MeMgBr followed by dehydration to give an olefin **Q**. Ozonolysis of **Q** leads to a dicarbonyl compound **R**, which undergoes intramolecular aldol reaction to give predominantly **S**.



16. The structure of the carbonyl compound **P** is

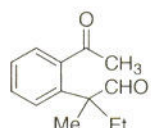
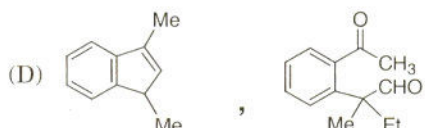
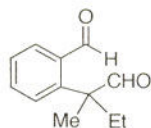
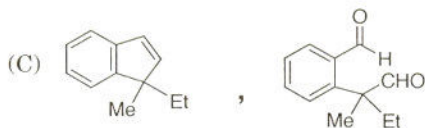
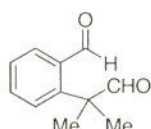
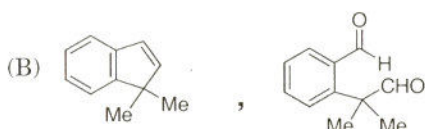
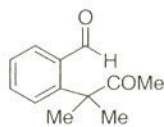
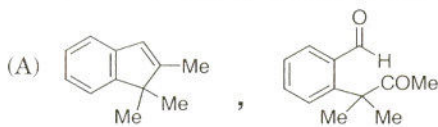


Answer



(A) (B) (C) (D)

17. The structures of the products **Q** and **R**, respectively, are

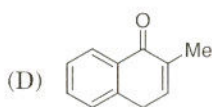
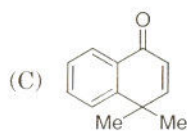
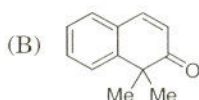
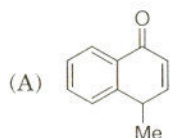


Answer



(A) (B) (C) (D)

18. The structure of the product **S** is



Answer

☐ (A)
 ☒ (B)
 ☐ (C)
 ☐ (D)

SECTION - IV

Matrix - Match Type

This section contains 2 questions. Each question contains statements given in two columns, which have to be matched. The statements in **Column I** are labelled A, B, C and D, while the statements in **Column II** are labelled p, q, r, s and t. Any given statement in **Column I** can have correct matching with **ONE OR MORE** statement(s) in **Column II**. The appropriate bubbles corresponding to the answers to these questions have to be darkened as illustrated in the following example:

If the correct matches are A – p, s and t; B – q and r; C – p and q; and D – s and t; then the correct darkening of bubbles will look like the following.

	p	q	r	s	t
A	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>
B	<input type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>
C	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
D	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>

19. Match each of the diatomic molecules in **Column I** with its property/properties in **Column II**.

Column I

- (A) B_2
 (B) N_2
 (C) O_2^-
 (D) O_2

Column II

- (p) Paramagnetic
 (q) Undergoes oxidation
 (r) Undergoes reduction
 (s) Bond order ≥ 2
 (t) Mixing of 's' and 'p' orbitals

Answer

	p	q	r	s	t
A	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>
B	<input type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>
C	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>
D	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>

20. Match each of the compounds in **Column I** with its characteristic reaction(s) in **Column II**.

Column I	Column II
(A) $\text{CH}_3\text{CH}_2\text{CH}_2\text{CN}$	(p) Reduction with $\text{Pd}-\text{C}/\text{H}_2$
(B) $\text{CH}_3\text{CH}_2\text{OCOCH}_3$	(q) Reduction with SnCl_2/HCl
(C) $\text{CH}_3-\text{CH}=\text{CH}-\text{CH}_2\text{OH}$	(r) Development of foul smell on treatment with chloroform and alcoholic KOH
(D) $\text{CH}_3\text{CH}_2\text{CH}_2\text{CH}_2\text{NH}_2$	(s) Reduction with diisobutylaluminium hydride (DIBAL-H)
	(t) Alkaline hydrolysis

Answer

	p	q	r	s	t
A	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>
B	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>
C	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
D	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>

PART II : MATHEMATICS

SECTION - I

Single Correct Choice Type

This section contains 8 multiple choice questions. Each question has 4 choices (A), (B), (C) and (D) for its answer, out of which **ONLY ONE** is correct.

21. Let $P(3, 2, 6)$ be a point in space and Q be a point on the line

$$\vec{r} = (\hat{i} - \hat{j} + 2\hat{k}) + \mu(-3\hat{i} + \hat{j} + 5\hat{k}).$$

Then the value of μ for which the vector \vec{PQ} is parallel to the plane $x - 4y + 3z = 1$ is

- (A) $\frac{1}{4}$ (B) $-\frac{1}{4}$ (C) $\frac{1}{8}$ (D) $-\frac{1}{8}$

Answer

- ☒ (A) ☐ (B) ☐ (C) ☐ (D)

22. Tangents drawn from the point $P(1, 8)$ to the circle

$$x^2 + y^2 - 6x - 4y - 11 = 0$$

touch the circle at the points A and B . The equation of the circumcircle of the triangle PAB is

- (A) $x^2 + y^2 + 4x - 6y + 19 = 0$ (B) $x^2 + y^2 - 4x - 10y + 19 = 0$
(C) $x^2 + y^2 - 2x + 6y - 29 = 0$ (D) $x^2 + y^2 - 6x - 4y + 19 = 0$

Answer

- ☐ (A) ☒ (B) ☐ (C) ☐ (D)

23. Let f be a non-negative function defined on the interval $[0, 1]$. If

$$\int_0^x \sqrt{1 - (f'(t))^2} dt = \int_0^x f(t) dt, \quad 0 \leq x \leq 1,$$

and $f(0) = 0$, then

- (A) $f\left(\frac{1}{2}\right) < \frac{1}{2}$ and $f\left(\frac{1}{3}\right) > \frac{1}{3}$ (B) $f\left(\frac{1}{2}\right) > \frac{1}{2}$ and $f\left(\frac{1}{3}\right) > \frac{1}{3}$
 (C) $f\left(\frac{1}{2}\right) < \frac{1}{2}$ and $f\left(\frac{1}{3}\right) < \frac{1}{3}$ (D) $f\left(\frac{1}{2}\right) > \frac{1}{2}$ and $f\left(\frac{1}{3}\right) < \frac{1}{3}$

Answer

- ☐ (A) ☐ (B) ☒ (C) ☐ (D)

24. Let $z = x + iy$ be a complex number where x and y are integers. Then the area of the rectangle whose vertices are the roots of the equation

$$z \bar{z}^3 + \bar{z} z^3 = 350$$

is

- (A) 48 (B) 32 (C) 40 (D) 80

Answer

- ☒ (A) ☐ (B) ☐ (C) ☐ (D)

25. The line passing through the extremity A of the major axis and extremity B of the minor axis of the ellipse

$$x^2 + 9y^2 = 9$$

meets its auxiliary circle at the point M . Then the area of the triangle with vertices at A, M and the origin O is

- (A) $\frac{31}{10}$ (B) $\frac{29}{10}$ (C) $\frac{21}{10}$ (D) $\frac{27}{10}$

Answer

- ☐ (A) ☐ (B) ☐ (C) ☒ (D)

26. If $\vec{a}, \vec{b}, \vec{c}$ and \vec{d} are unit vectors such that

$$(\vec{a} \times \vec{b}) \cdot (\vec{c} \times \vec{d}) = 1$$

$$\text{and } \vec{a} \cdot \vec{c} = \frac{1}{2},$$

then

- (A) $\vec{a}, \vec{b}, \vec{c}$ are non-coplanar (B) $\vec{b}, \vec{c}, \vec{d}$ are non-coplanar
 (C) \vec{b}, \vec{d} are non-parallel (D) \vec{a}, \vec{d} are parallel and \vec{b}, \vec{c} are parallel

Answer

- ☐ (A) ☐ (B) ☒ (C) ☐ (D)

27. Let $z = \cos \theta + i \sin \theta$. Then the value of

$$\sum_{m=1}^{15} \operatorname{Im}(z^{2m-1})$$

at $\theta = 2^\circ$ is

- (A) $\frac{1}{\sin 2^\circ}$ (B) $\frac{1}{3 \sin 2^\circ}$ (C) $\frac{1}{2 \sin 2^\circ}$ (D) $\frac{1}{4 \sin 2^\circ}$

Answer

- ☐ (A) ☐ (B) ☐ (C) ☒ (D)

28. The number of seven digit integers, with sum of the digits equal to 10 and formed by using the digits 1, 2 and 3 only, is

(A) 55 (B) 66 (C) 77 (D) 88

Answer



(A) (B) (C) (D)

SECTION – II

Multiple Correct Choice Type

This section contains 4 multiple choice questions. Each question has 4 choices (A), (B), (C) and (D) for its answer, out of which **ONE OR MORE** is/are correct.

29. Area of the region bounded by the curve $y = e^x$ and lines $x = 0$ and $y = e$ is

(A) $e - 1$ (B) $\int_1^e \ln(e + 1 - y) dy$
 (C) $e - \int_0^1 e^x dx$ (D) $\int_1^e \ln y dy$

Answer



(A) (B) (C) (D)

30. Let

$$L = \lim_{x \rightarrow 0} \frac{a - \sqrt{a^2 - x^2} - \frac{x^2}{4}}{x^4}, \quad a > 0.$$

If L is finite, then

(A) $a = 2$ (B) $a = 1$ (C) $L = \frac{1}{64}$ (D) $L = \frac{1}{32}$

Answer



(A) (B) (C) (D)

31. In a triangle ABC with fixed base BC , the vertex A moves such that

$$\cos B + \cos C = 4 \sin^2 \frac{A}{2}.$$

If a, b and c denote the lengths of the sides of the triangle opposite to the angles A, B and C , respectively, then

(A) $b + c = 4a$
 (B) $b + c = 2a$
 (C) locus of point A is an ellipse
 (D) locus of point A is a pair of straight lines

Answer



(A) (B) (C) (D)

32. If

$$\frac{\sin^4 x}{2} + \frac{\cos^4 x}{3} = \frac{1}{5},$$

then

(A) $\tan^2 x = \frac{2}{3}$

(B) $\frac{\sin^8 x}{8} + \frac{\cos^8 x}{27} = \frac{1}{125}$

(C) $\tan^2 x = \frac{1}{3}$

(D) $\frac{\sin^8 x}{8} + \frac{\cos^8 x}{27} = \frac{2}{125}$

Answer



(A) (B) (C) (D)

SECTION - III

Comprehension Type

This section contains 2 groups of questions. Each group has 3 multiple choice questions based on a paragraph. Each question has 4 choices (A), (B), (C) and (D) for its answer, out of which **ONLY ONE** is correct.

Paragraph for Question Nos. 33 to 35

Let \mathcal{A} be the set of all 3×3 symmetric matrices all of whose entries are either 0 or 1. Five of these entries are 1 and four of them are 0.

33. The number of matrices in \mathcal{A} is

(A) 12

(B) 6

(C) 9

(D) 3

Answer



(A) (B) (C) (D)

34. The number of matrices A in \mathcal{A} for which the system of linear equations

$$A \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$$

has a unique solution, is

(A) less than 4

(B) at least 4 but less than 7

(C) at least 7 but less than 10

(D) at least 10

Answer



(A) (B) (C) (D)

35. The number of matrices A in \mathcal{A} for which the system of linear equations

$$A \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 1 \\ 0 \\ 0 \end{bmatrix}$$

is inconsistent, is

(A) 0

(B) more than 2

(C) 2

(D) 1

Answer



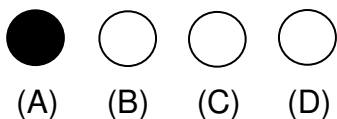
(A) (B) (C) (D)

A fair die is tossed repeatedly until a six is obtained. Let X denote the number of tosses required.

36. The probability that $X = 3$ equals

- (A) $\frac{25}{216}$ (B) $\frac{25}{36}$ (C) $\frac{5}{36}$ (D) $\frac{125}{216}$

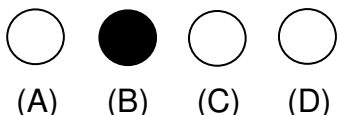
Answer



37. The probability that $X \geq 3$ equals

- (A) $\frac{125}{216}$ (B) $\frac{25}{36}$ (C) $\frac{5}{36}$ (D) $\frac{25}{216}$

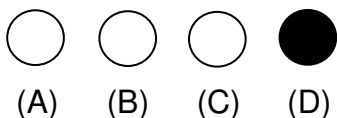
Answer



38. The conditional probability that $X \geq 6$ given $X > 3$ equals

- (A) $\frac{125}{216}$ (B) $\frac{25}{216}$ (C) $\frac{5}{36}$ (D) $\frac{25}{36}$

Answer



SECTION – IV

Matrix – Match Type

This section contains 2 questions. Each question contains statements given in two columns, which have to be matched. The statements in **Column I** are labelled A, B, C and D, while the statements in **Column II** are labelled p, q, r, s and t. Any given statement in **Column I** can have correct matching with **ONE OR MORE** statement(s) in **Column II**. The appropriate bubbles corresponding to the answers to these questions have to be darkened as illustrated in the following example:

If the correct matches are A – p, s and t; B – q and r; C – p and q; and D – s and t; then the correct darkening of bubbles will look like the following.

	p	q	r	s	t
A	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>
B	<input type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>
C	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
D	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>

39. Match the statements/expressions in **Column I** with the open intervals in **Column II**.

Column I	Column II
(A) Interval contained in the domain of definition of non-zero solutions of the differential equation $(x-3)^2 y' + y = 0$	(p) $\left(-\frac{\pi}{2}, \frac{\pi}{2}\right)$
(B) Interval containing the value of the integral $\int_1^5 (x-1)(x-2)(x-3)(x-4)(x-5) dx$	(q) $\left(0, \frac{\pi}{2}\right)$
(C) Interval in which at least one of the points of local maximum of $\cos^2 x + \sin x$ lies	(r) $\left(\frac{\pi}{8}, \frac{5\pi}{4}\right)$
(D) Interval in which $\tan^{-1}(\sin x + \cos x)$ is increasing	(s) $\left(0, \frac{\pi}{8}\right)$
	(t) $(-\pi, \pi)$

Answer

	p	q	r	s	t
A	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>
B	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>
C	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>
D	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>

40. Match the conics in **Column I** with the statements/expressions in **Column II**.

Column I	Column II
(A) Circle	(p) The locus of the point (h, k) for which the line $hx + ky = 1$ touches the circle $x^2 + y^2 = 4$
(B) Parabola	(q) Points z in the complex plane satisfying $ z+2 - z-2 = \pm 3$
(C) Ellipse	(r) Points of the conic have parametric representation $x = \sqrt{3} \left(\frac{1-t^2}{1+t^2} \right), y = \frac{2t}{1+t^2}$
(D) Hyperbola	(s) The eccentricity of the conic lies in the interval $1 \leq e < \infty$
	(t) Points z in the complex plane satisfying $\operatorname{Re}(z+1)^2 = z ^2 + 1$

Answer

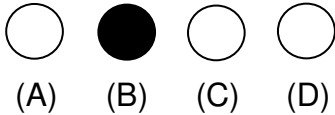
	p	q	r	s	t
A	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
B	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>
C	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>
D	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>

PART III : PHYSICS**SECTION - I****Single Correct Choice Type**

This section contains 8 multiple choice questions. Each question has 4 choices (A), (B), (C) and (D) for its answer, out of which **ONLY ONE** is correct.

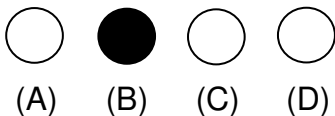
41. Three concentric metallic spherical shells of radii $R, 2R, 3R$, are given charges Q_1, Q_2, Q_3 , respectively. It is found that the surface charge densities on the outer surfaces of the shells are equal. Then, the ratio of the charges given to the shells, $Q_1 : Q_2 : Q_3$, is

(A) 1 : 2 : 3 (B) 1 : 3 : 5 (C) 1 : 4 : 9 (D) 1 : 8 : 18

Answer

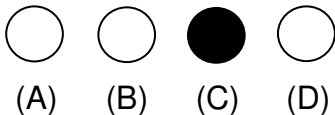
42. A block of base $10 \text{ cm} \times 10 \text{ cm}$ and height 15 cm is kept on an inclined plane. The coefficient of friction between them is $\sqrt{3}$. The inclination θ of this inclined plane from the horizontal plane is gradually increased from 0° . Then

(A) at $\theta = 30^\circ$, the block will start sliding down the plane
 (B) the block will remain at rest on the plane up to certain θ and then it will topple
 (C) at $\theta = 60^\circ$, the block will start sliding down the plane and continue to do so at higher angles
 (D) at $\theta = 60^\circ$, the block will start sliding down the plane and on further increasing θ , it will topple at certain θ

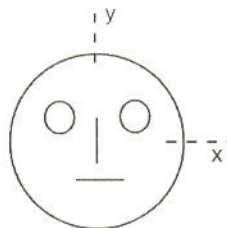
Answer

43. A ball is dropped from a height of 20 m above the surface of water in a lake. The refractive index of water is $4/3$. A fish inside the lake, in the line of fall of the ball, is looking at the ball. At an instant, when the ball is 12.8 m above the water surface, the fish sees the speed of ball as [Take $g = 10 \text{ m/s}^2$.]

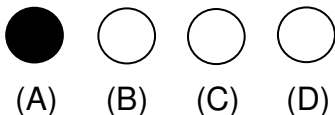
(A) 9 m/s (B) 12 m/s (C) 16 m/s (D) 21.33 m/s

Answer

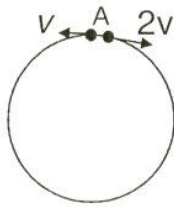
44. Look at the drawing given in the figure which has been drawn with ink of uniform line-thickness. The mass of ink used to draw each of the two inner circles, and each of the two line segments is m . The mass of the ink used to draw the outer circle is $6m$. The coordinates of the centres of the different parts are: outer circle $(0, 0)$, left inner circle $(-a, a)$, right inner circle (a, a) , vertical line $(0, 0)$ and horizontal line $(0, -a)$. The y -coordinate of the centre of mass of the ink in this drawing is



(A) $\frac{a}{10}$ (B) $\frac{a}{8}$ (C) $\frac{a}{12}$ (D) $\frac{a}{3}$

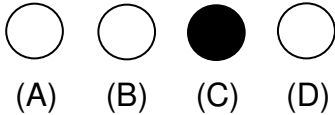
Answer

45. Two small particles of equal masses start moving in opposite directions from a point A in a horizontal circular orbit. Their tangential velocities are v and $2v$, respectively, as shown in the figure. Between collisions, the particles move with constant speeds. After making how many elastic collisions, other than that at A, these two particles will again reach the point A?

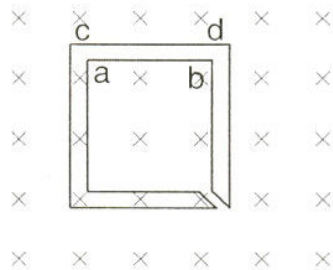


- (A) 4 (B) 3 (C) 2 (D) 1

Answer

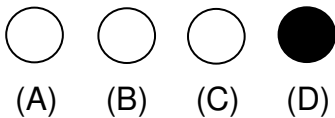


46. The figure shows certain wire segments joined together to form a coplanar loop. The loop is placed in a perpendicular magnetic field in the direction going into the plane of the figure. The magnitude of the field increases with time. I_1 and I_2 are the currents in the segments **ab** and **cd**. Then,

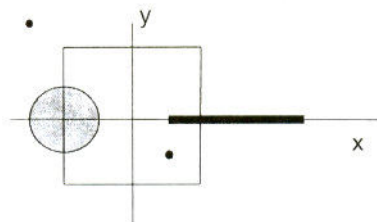


- (A) $I_1 > I_2$
 (B) $I_1 < I_2$
 (C) I_1 is in the direction **ba** and I_2 is in the direction **cd**
 (D) I_1 is in the direction **ab** and I_2 is in the direction **dc**

Answer

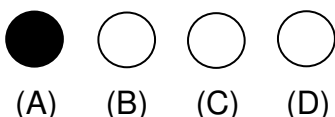


47. A disk of radius $a/4$ having a uniformly distributed charge $6C$ is placed in the x - y plane with its centre at $(-a/2, 0, 0)$. A rod of length a carrying a uniformly distributed charge $8C$ is placed on the x -axis from $x = a/4$ to $x = 5a/4$. Two point charges $-7C$ and $3C$ are placed at $(a/4, -a/4, 0)$ and $(-3a/4, 3a/4, 0)$, respectively. Consider a cubical surface formed by six surfaces $x = \pm a/2$, $y = \pm a/2$, $z = \pm a/2$. The electric flux through this cubical surface is

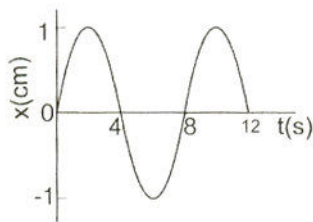


- (A) $\frac{-2C}{\epsilon_0}$ (B) $\frac{2C}{\epsilon_0}$ (C) $\frac{10C}{\epsilon_0}$ (D) $\frac{12C}{\epsilon_0}$

Answer



48. The x - t graph of a particle undergoing simple harmonic motion is shown below. The acceleration of the particle at $t = 4/3$ s is



- (A) $\frac{\sqrt{3}}{32} \pi^2 \text{ cm/s}^2$ (B) $-\frac{\pi^2}{32} \text{ cm/s}^2$
 (C) $\frac{\pi^2}{32} \text{ cm/s}^2$ (D) $-\frac{\sqrt{3}}{32} \pi^2 \text{ cm/s}^2$

Answer

- ☐ ☐ ☐ ☒
 (A) (B) (C) (D)

SECTION - II

Multiple Correct Choice Type

This section contains 4 multiple choice questions. Each question has 4 choices (A), (B), (C) and (D) for its answer, out of which **ONE OR MORE** is/are correct.

49. If the resultant of all the external forces acting on a system of particles is zero, then from an inertial frame, one can surely say that
- (A) linear momentum of the system does not change in time
 (B) kinetic energy of the system does not change in time
 (C) angular momentum of the system does not change in time
 (D) potential energy of the system does not change in time

Answer

- ☒ ☐ ☐ ☐
 (A) (B) (C) (D)

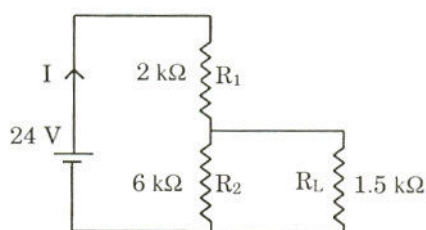
50. A student performed the experiment of determination of focal length of a concave mirror by u-v method using an optical bench of length 1.5 meter. The focal length of the mirror used is 24 cm. The maximum error in the location of the image can be 0.2 cm. The 5 sets of (u, v) values recorded by the student (in cm) are: (42, 56), (48, 48), (60, 40), (66, 33), (78, 39). The data set(s) that **cannot** come from experiment and is (are) incorrectly recorded, is (are)

- (A) (42, 56) (B) (48, 48) (C) (66, 33) (D) (78, 39)

Answer

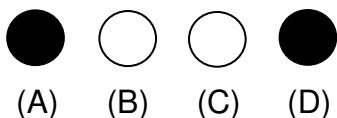
- ☐ ☐ ☒ ☒
 (A) (B) (C) (D)

51. For the circuit shown in the figure



- (A) the current I through the battery is 7.5 mA
 (B) the potential difference across R_L is 18 V
 (C) ratio of powers dissipated in R_1 and R_2 is 3
 (D) if R_1 and R_2 are interchanged, magnitude of the power dissipated in R_L will decrease by a factor of 9

Answer

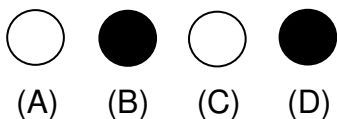


(A) (B) (C) (D)

52. C_v and C_p denote the molar specific heat capacities of a gas at constant volume and constant pressure, respectively. Then

- (A) $C_p - C_v$ is larger for a diatomic ideal gas than for a monoatomic ideal gas
 (B) $C_p + C_v$ is larger for a diatomic ideal gas than for a monoatomic ideal gas
 (C) C_p / C_v is larger for a diatomic ideal gas than for a monoatomic ideal gas
 (D) $C_p \cdot C_v$ is larger for a diatomic ideal gas than for a monoatomic ideal gas

Answer



(A) (B) (C) (D)

SECTION - III

Comprehension Type

This section contains 2 groups of questions. Each group has 3 multiple choice questions based on a paragraph. Each question has 4 choices (A), (B), (C) and (D) for its answer, out of which **ONLY ONE** is correct.

Paragraph for Question Nos. 53 to 55

Scientists are working hard to develop nuclear fusion reactor. Nuclei of heavy hydrogen, ${}^2_1\text{H}$, known as deuteron and denoted by D, can be thought of as a candidate for fusion reactor. The D-D reaction is ${}^2_1\text{H} + {}^2_1\text{H} \rightarrow {}^3_2\text{He} + n + \text{energy}$. In the core of fusion reactor, a gas of heavy hydrogen is fully ionized into deuteron nuclei and electrons. This collection of ${}^2_1\text{H}$ nuclei and electrons is known as plasma. The nuclei move randomly in the reactor core and occasionally come close enough for nuclear fusion to take place. Usually, the temperatures in the reactor core are too high and no material wall can be used to confine the plasma. Special techniques are used which confine the plasma for a time t_0 before the particles fly away from the core. If n is the density (number/volume) of deuterons, the product nt_0 is called Lawson number. In one of the criteria, a reactor is termed successful if Lawson number is greater than $5 \times 10^{14} \text{ s/cm}^3$.

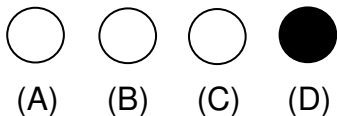
It may be helpful to use the following: Boltzmann constant $k = 8.6 \times 10^{-5} \text{ eV/K}$;

$$\frac{e^2}{4\pi\epsilon_0} = 1.44 \times 10^{-9} \text{ eVm.}$$

53. In the core of nuclear fusion reactor, the gas becomes plasma because of

- (A) strong nuclear force acting between the deuterons
 (B) Coulomb force acting between the deuterons
 (C) Coulomb force acting between deuteron-electron pairs
 (D) the high temperature maintained inside the reactor core

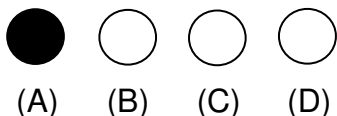
Answer



54. Assume that two deuteron nuclei in the core of fusion reactor at temperature T are moving towards each other, each with kinetic energy $1.5 kT$, when the separation between them is large enough to neglect Coulomb potential energy. Also neglect any interaction from other particles in the core. The minimum temperature T required for them to reach a separation of 4×10^{-15} m is in the range

- (A) $1.0 \times 10^9 \text{ K} < T < 2.0 \times 10^9 \text{ K}$
 (B) $2.0 \times 10^9 \text{ K} < T < 3.0 \times 10^9 \text{ K}$
 (C) $3.0 \times 10^9 \text{ K} < T < 4.0 \times 10^9 \text{ K}$
 (D) $4.0 \times 10^9 \text{ K} < T < 5.0 \times 10^9 \text{ K}$

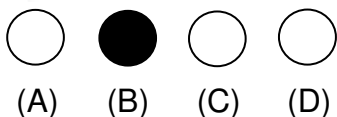
Answer



55. Results of calculations for four different designs of a fusion reactor using D-D reaction are given below. Which of these is most promising based on Lawson criterion?

- (A) deuteron density = $2.0 \times 10^{12} \text{ cm}^{-3}$, confinement time = $5.0 \times 10^{-3} \text{ s}$
 (B) deuteron density = $8.0 \times 10^{14} \text{ cm}^{-3}$, confinement time = $9.0 \times 10^{-1} \text{ s}$
 (C) deuteron density = $4.0 \times 10^{23} \text{ cm}^{-3}$, confinement time = $1.0 \times 10^{-11} \text{ s}$
 (D) deuteron density = $1.0 \times 10^{24} \text{ cm}^{-3}$, confinement time = $4.0 \times 10^{-12} \text{ s}$

Answer



Paragraph for Question Nos. 56 to 58

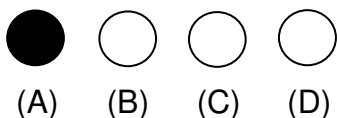
When a particle is restricted to move along x -axis between $x = 0$ and $x = a$, where a is of nanometer dimension, its energy can take only certain specific values. The allowed energies of the particle moving in such a restricted region, correspond to the formation of standing waves with nodes at its ends $x = 0$ and $x = a$. The wavelength of this standing wave is related to the linear momentum p of the particle according to the de Broglie relation. The energy of the particle of mass m is related to its linear momentum as $E = \frac{p^2}{2m}$. Thus, the energy of the particle can be denoted by a quantum number ' n ' taking values 1, 2, 3, ... ($n = 1$, called the ground state) corresponding to the number of loops in the standing wave.

Use the model described above to answer the following three questions for a particle moving in the line $x = 0$ to $x = a$. Take $\hbar = 6.6 \times 10^{-34} \text{ J s}$ and $e = 1.6 \times 10^{-19} \text{ C}$.

56. The allowed energy for the particle for a particular value of n is proportional to

- (A) a^{-2} (B) $a^{-3/2}$ (C) a^{-1} (D) a^2

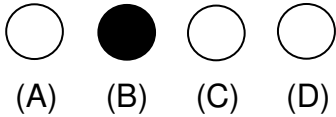
Answer



57. If the mass of the particle is $m = 1.0 \times 10^{-30}$ kg and $a = 6.6$ nm, the energy of the particle in its ground state is closest to

(A) 0.8 meV (B) 8 meV (C) 80 meV (D) 800 meV

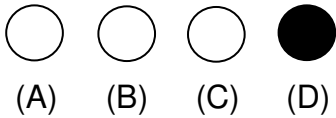
Answer



58. The speed of the particle, that can take discrete values, is proportional to

(A) $n^{-3/2}$ (B) n^{-1} (C) $n^{1/2}$ (D) n

Answer



SECTION – IV

Matrix – Match Type

This section contains 2 questions. Each question contains statements given in two columns, which have to be matched. The statements in **Column I** are labelled A, B, C and D, while the statements in **Column II** are labelled p, q, r, s and t. Any given statement in **Column I** can have correct matching with **ONE OR MORE** statement(s) in **Column II**. The appropriate bubbles corresponding to the answers to these questions have to be darkened as illustrated in the following example:

If the correct matches are A – p, s and t; B – q and r; C – p and q; and D – s and t; then the correct darkening of bubbles will look like the following.

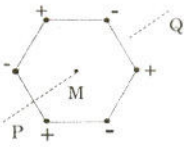

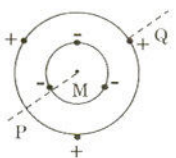
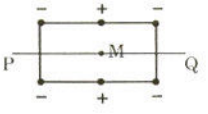
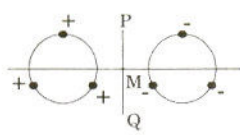
	p	q	r	s	t
A	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>
B	<input type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>
C	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
D	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>

59. Six point charges, each of the same magnitude q , are arranged in different manners as shown in **Column II**. In each case, a point M and a line PQ passing through M are shown. Let E be the electric field and V be the electric potential at M (potential at infinity is zero) due to the given charge distribution when it is at rest. Now, the whole system is set into rotation with a constant angular velocity about the line PQ . Let B be the magnetic field at M and μ be the magnetic moment of the system in this condition. Assume each rotating charge to be equivalent to a steady current.

Column I

- (A) $E = 0$
 (B) $V \neq 0$
 (C) $B = 0$
 (D) $\mu \neq 0$

Column II

- (p)  Charges are at the corners of a regular hexagon. M is at the centre of the hexagon. PQ is perpendicular to the plane of the hexagon.
- (q)  Charges are on a line perpendicular to PQ at equal intervals. M is the mid-point between the two innermost charges.
- (r)  Charges are placed on two coplanar insulating rings at equal intervals. M is the common centre of the rings. PQ is perpendicular to the plane of the rings.
- (s)  Charges are placed at the corners of a rectangle of sides a and $2a$ and at the mid points of the longer sides. M is at the centre of the rectangle. PQ is parallel to the longer sides.
- (t)  Charges are placed on two coplanar, identical insulating rings at equal intervals. M is the mid-point between the centres of the rings. PQ is perpendicular to the line joining the centres and coplanar to the rings.

Answer

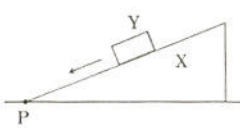
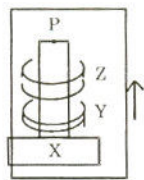
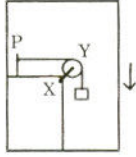
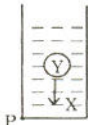
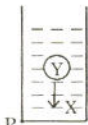
	p	q	r	s	t
A	<input checked="" type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>
B	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>
C	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>
D	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>

60. **Column II** shows five systems in which two objects are labelled as X and Y. Also in each case a point P is shown. **Column I** gives some statements about X and/or Y. Match these statements to the appropriate system(s) from **Column II**.

Column I

- (A) The force exerted by X on Y has a magnitude Mg .
 (B) The gravitational potential energy of X is continuously increasing.
 (C) Mechanical energy of the system X + Y is continuously decreasing.
 (D) The torque of the weight of Y about point P is zero.

Column II

- (p)  Block Y of mass M left on a fixed inclined plane X, slides on it with a constant velocity.
- (q)  Two ring magnets Y and Z, each of mass M , are kept in frictionless vertical plastic stand so that they repel each other. Y rests on the base X and Z hangs in air in equilibrium. P is the topmost point of the stand on the common axis of the two rings. The whole system is in a lift that is going up with a constant velocity.
- (r)  A pulley Y of mass m_0 is fixed to a table through a clamp X. A block of mass M hangs from a string that goes over the pulley and is fixed at point P of the table. The whole system is kept in a lift that is going down with a constant velocity.
- (s)  A sphere Y of mass M is put in a nonviscous liquid X kept in a container at rest. The sphere is released and it moves down in the liquid.
- (t)  A sphere Y of mass M is falling with its terminal velocity in a viscous liquid X kept in a container.

Answer

	p	q	r	s	t
A	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
B	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>
C	<input checked="" type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>
D	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>

PART I : CHEMISTRY

SECTION - I

Single Correct Choice Type

This section contains 4 multiple choice questions. Each question has 4 choices (A), (B), (C) and (D) for its answer, out of which **ONLY ONE** is correct.

1. For a first order reaction $A \rightarrow P$, the temperature (T) dependent rate constant (k) was found to follow the equation $\log k = -(2000) \frac{1}{T} + 6.0$. The pre-exponential factor A and the activation energy E_a , respectively, are
- (A) $1.0 \times 10^6 \text{ s}^{-1}$ and 9.2 kJ mol^{-1}
 (B) 6.0 s^{-1} and 16.6 kJ mol^{-1}
 (C) $1.0 \times 10^6 \text{ s}^{-1}$ and 16.6 kJ mol^{-1}
 (D) $1.0 \times 10^6 \text{ s}^{-1}$ and 38.3 kJ mol^{-1}

Answer

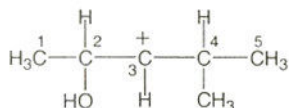
- ☐ (A) ☐ (B) ☐ (C) ☒ (D)

2. The spin only magnetic moment value (in Bohr magneton units) of $\text{Cr}(\text{CO})_6$ is
- (A) 0 (B) 2.84 (C) 4.90 (D) 5.92

Answer

- ☒ (A) ☐ (B) ☐ (C) ☐ (D)

3. In the following carbocation, H/CH_3 that is most likely to migrate to the positively charged carbon is

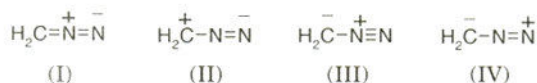


- (A) CH_3 at C-4 (B) H at C-4
 (C) CH_3 at C-2 (D) H at C-2

Answer

- ☐ (A) ☐ (B) ☐ (C) ☒ (D)

4. The correct stability order of the following resonance structures is



- (A) (I) > (II) > (IV) > (III) (B) (I) > (III) > (II) > (IV)
 (C) (II) > (I) > (III) > (IV) (D) (III) > (I) > (IV) > (II)

Answer

- ☐ (A) ☒ (B) ☐ (C) ☐ (D)

SECTION – II

Multiple Correct Choice Type

This section contains 5 multiple choice questions. Each question has 4 choices (A), (B), (C) and (D) for its answer, out of which **ONE OR MORE** is/are correct.

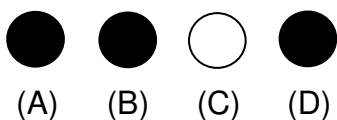
5. For the reduction of NO_3^- ion in an aqueous solution, E^0 is +0.96 V. Values of E^0 for some metal ions are given below



The pair(s) of metals that is(are) oxidized by NO_3^- in aqueous solution is(are)

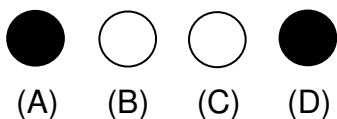
- (A) V and Hg (B) Hg and Fe
(C) Fe and Au (D) Fe and V

Answer



6. Among the following, the state function(s) is(are)
- (A) Internal energy (B) Irreversible expansion work
(C) Reversible expansion work (D) Molar enthalpy

Answer



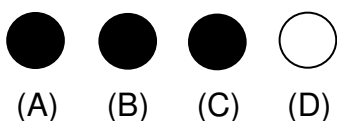
7. In the reaction



the amine(s) **X** is(are)

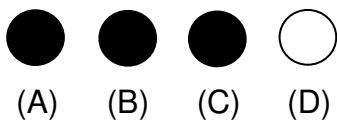
- (A) NH_3 (B) CH_3NH_2
(C) $(\text{CH}_3)_2\text{NH}$ (D) $(\text{CH}_3)_3\text{N}$

Answer

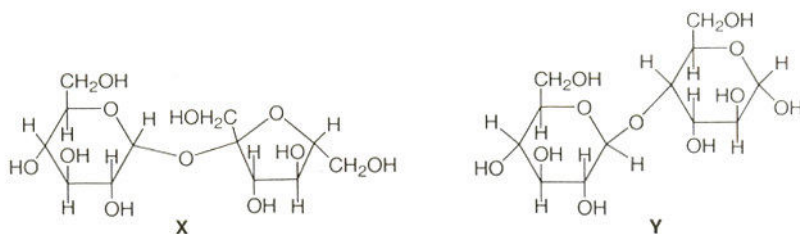


8. The nitrogen oxide(s) that contain(s) N-N bond(s) is(are)
- (A) N_2O (B) N_2O_3 (C) N_2O_4 (D) N_2O_5

Answer

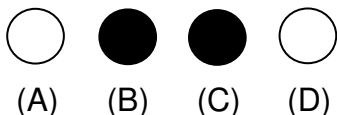


9. The correct statement(s) about the following sugars **X** and **Y** is(are)



- (A) **X** is a reducing sugar and **Y** is a non-reducing sugar
 (B) **X** is a non-reducing sugar and **Y** is a reducing sugar
 (C) The glucosidic linkages in **X** and **Y** are α and β , respectively
 (D) The glucosidic linkages in **X** and **Y** are β and α , respectively

Answer



SECTION – III

Matrix – Match Type

This section contains 2 questions. Each question contains statements given in two columns, which have to be matched. The statements in **Column I** are labelled A, B, C and D, while the statements in **Column II** are labelled p, q, r, s and t. Any given statement in **Column I** can have correct matching with **ONE OR MORE** statement(s) in **Column II**. The appropriate bubbles corresponding to the answers to these questions have to be darkened as illustrated in the following example:

If the correct matches are A – p, s and t; B – q and r; C – p and q; and D – s and t; then the correct darkening of bubbles will look like the following.

	p	q	r	s	t
A	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>
B	<input type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>
C	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
D	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>

10. Match each of the reactions given in **Column I** with the corresponding product(s) given in **Column II**.

Column I	Column II
(A) $\text{Cu} + \text{dil HNO}_3$	(p) NO
(B) $\text{Cu} + \text{conc HNO}_3$	(q) NO_2
(C) $\text{Zn} + \text{dil HNO}_3$	(r) N_2O
(D) $\text{Zn} + \text{conc HNO}_3$	(s) $\text{Cu}(\text{NO}_3)_2$
	(t) $\text{Zn}(\text{NO}_3)_2$

Answer

	p	q	r	s	t
A	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>
B	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>
C	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>
D	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>

11. Match each of the compounds given in **Column I** with the reaction(s), that they can undergo, given in **Column II**.

Column I	Column II
(A)	(p) Nucleophilic substitution
(B)	(q) Elimination
(C)	(r) Nucleophilic addition
(D)	(s) Esterification with acetic anhydride
	(t) Dehydrogenation

Answer

	p	q	r	s	t
A	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>
B	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>
C	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>
D	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>

SECTION - IV

Integer Answer Type

This section contains 8 questions. The answer to each of the questions is a single-digit integer, ranging from 0 to 9. The appropriate bubbles below the respective question numbers in the ORS have to be darkened. For example, if the correct answers to question numbers X, Y, Z and W (say) are 6, 0, 9 and 2, respectively, then the correct darkening of bubbles will look like the following:

X	Y	Z	W
<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>
<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>
<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>

12. In a constant volume calorimeter, 3.5 g of a gas with molecular weight 28 was burnt in excess oxygen at 298.0 K. The temperature of the calorimeter was found to increase from 298.0 K to 298.45 K due to the combustion process. Given that the heat capacity of the calorimeter is 2.5 kJ K^{-1} , the numerical value for the enthalpy of combustion of the gas in kJ mol^{-1} is

Answer

☐ 0
 ☐ 1
 ☐ 2
 ☐ 3
 ☐ 4
 ☐ 5
 ☐ 6
 ☐ 7
 ☐ 8
 ☒ 9

13. At 400 K, the root mean square (rms) speed of a gas **X** (molecular weight = 40) is equal to the most probable speed of gas **Y** at 60 K. The molecular weight of the gas **Y** is

Answer

- (0) (1) (2) (3) (4) (5) (6) (7) (8) (9)

14. The dissociation constant of a substituted benzoic acid at 25°C is 1.0×10^{-4} . The pH of a 0.01 M solution of its sodium salt is

Answer

- (0) (1) (2) (3) (4) (5) (6) (7) (8) (9)

15. The total number of α and β particles emitted in the nuclear reaction ${}_{92}^{238}\text{U} \rightarrow {}_{82}^{214}\text{Pb}$ is

Answer

- (0) (1) (2) (3) (4) (5) (6) (7) (8) (9)

16. The oxidation number of Mn in the product of alkaline oxidative fusion of MnO_2 is

Answer

- (0) (1) (2) (3) (4) (5) (6) (7) (8) (9)

17. The number of water molecule(s) directly bonded to the metal centre in $\text{CuSO}_4 \cdot 5\text{H}_2\text{O}$ is

Answer

- (0) (1) (2) (3) (4) (5) (6) (7) (8) (9)

18. The coordination number of Al in the crystalline state of AlCl_3 is

Answer

- (0) (1) (2) (3) (4) (5) (6) (7) (8) (9)

19. The total number of cyclic structural as well as stereo isomers possible for a compound with the molecular formula C_5H_{10} is

Answer

- (0) (1) (2) (3) (4) (5) (6) (7) (8) (9)

PART II : MATHEMATICS

SECTION - I

Single Correct Choice Type

This section contains 4 multiple choice questions. Each question has 4 choices (A), (B), (C) and (D) for its answer, out of which **ONLY ONE** is correct.

20. If the sum of first n terms of an A.P. is cn^2 , then the sum of squares of these n terms is

(A) $\frac{n(4n^2 - 1)c^2}{6}$

(B) $\frac{n(4n^2 + 1)c^2}{3}$

(C) $\frac{n(4n^2 - 1)c^2}{3}$

(D) $\frac{n(4n^2 + 1)c^2}{6}$

Answer

- (A) (B) (C) (D)

21. A line with positive direction cosines passes through the point $P(2, -1, 2)$ and makes equal angles with the coordinate axes. The line meets the plane

$$2x + y + z = 9$$

at point Q . The length of the line segment PQ equals

- (A) 1 (B) $\sqrt{2}$ (C) $\sqrt{3}$ (D) 2

Answer



(A) (B) (C) (D)

22. The normal at a point P on the ellipse $x^2 + 4y^2 = 16$ meets the x -axis at Q . If M is the mid point of the line segment PQ , then the locus of M intersects the latus rectums of the given ellipse at the points

- (A) $\left(\pm \frac{3\sqrt{5}}{2}, \pm \frac{2}{7}\right)$ (B) $\left(\pm \frac{3\sqrt{5}}{2}, \pm \frac{\sqrt{19}}{4}\right)$
 (C) $\left(\pm 2\sqrt{3}, \pm \frac{1}{7}\right)$ (D) $\left(\pm 2\sqrt{3}, \pm \frac{4\sqrt{3}}{7}\right)$

Answer



(A) (B) (C) (D)

23. The locus of the orthocentre of the triangle formed by the lines

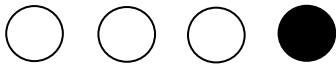
$$(1+p)x - py + p(1+p) = 0,$$

$$(1+q)x - qy + q(1+q) = 0,$$

and $y = 0$, where $p \neq q$, is

- (A) a hyperbola (B) a parabola
 (C) an ellipse (D) a straight line

Answer



(A) (B) (C) (D)

SECTION - II

Multiple Correct Choice Type

This section contains 5 multiple choice questions. Each question has 4 choices (A), (B), (C) and (D) for its answer, out of which **ONE OR MORE** is/are correct.

24. If

$$I_n = \int_{-\pi}^{\pi} \frac{\sin nx}{(1 + \pi^x) \sin x} dx, \quad n = 0, 1, 2, \dots,$$

then

- (A) $I_n = I_{n+2}$ (B) $\sum_{m=1}^{10} I_{2m+1} = 10\pi$
 (C) $\sum_{m=1}^{10} I_{2m} = 0$ (D) $I_n = I_{n+1}$

Answer

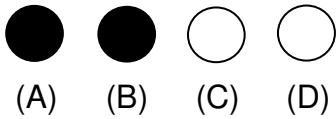


(A) (B) (C) (D)

25. An ellipse intersects the hyperbola $2x^2 - 2y^2 = 1$ orthogonally. The eccentricity of the ellipse is reciprocal of that of the hyperbola. If the axes of the ellipse are along the coordinate axes, then

- (A) Equation of ellipse is $x^2 + 2y^2 = 2$
 (B) The foci of ellipse are $(\pm 1, 0)$
 (C) Equation of ellipse is $x^2 + 2y^2 = 4$
 (D) The foci of ellipse are $(\pm\sqrt{2}, 0)$

Answer

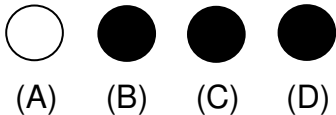


26. For the function

$$f(x) = x \cos \frac{1}{x}, \quad x \geq 1,$$

- (A) for at least one x in the interval $[1, \infty)$, $f(x+2) - f(x) < 2$
 (B) $\lim_{x \rightarrow \infty} f'(x) = 1$
 (C) for all x in the interval $[1, \infty)$, $f(x+2) - f(x) > 2$
 (D) $f'(x)$ is strictly decreasing in the interval $[1, \infty)$

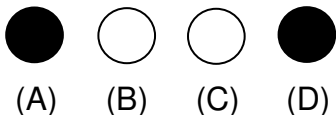
Answer



27. The tangent PT and the normal PN to the parabola $y^2 = 4ax$ at a point P on it meet its axis at points T and N , respectively. The locus of the centroid of the triangle PTN is a parabola whose

- (A) vertex is $\left(\frac{2a}{3}, 0\right)$ (B) directrix is $x = 0$
 (C) latus rectum is $\frac{2a}{3}$ (D) focus is $(a, 0)$

Answer



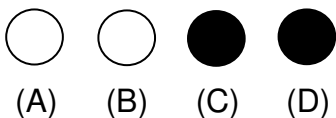
28. For $0 < \theta < \frac{\pi}{2}$, the solution(s) of

$$\sum_{m=1}^6 \operatorname{cosec} \left(\theta + \frac{(m-1)\pi}{4} \right) \operatorname{cosec} \left(\theta + \frac{m\pi}{4} \right) = 4\sqrt{2}$$

is(are)

- (A) $\frac{\pi}{4}$ (B) $\frac{\pi}{6}$ (C) $\frac{\pi}{12}$ (D) $\frac{5\pi}{12}$

Answer



SECTION - III

Matrix - Match Type

This section contains 2 questions. Each question contains statements given in two columns, which have to be matched. The statements in **Column I** are labelled A, B, C and D, while the statements in **Column II** are labelled p, q, r, s and t. Any given statement in **Column I** can have correct matching with **ONE OR MORE** statement(s) in **Column II**. The appropriate bubbles corresponding to the answers to these questions have to be darkened as illustrated in the following example:

If the correct matches are A – p, s and t; B – q and r; C – p and q; and D – s and t; then the correct darkening of bubbles will look like the following.

	p	q	r	s	t
A	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>
B	<input type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>
C	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
D	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>

29. Match the statements/expressions given in **Column I** with the values given in **Column II**.

Column I

- (A) Root(s) of the equation
 $2\sin^2 \theta + \sin^2 2\theta = 2$
- (B) Points of discontinuity of the function
 $f(x) = \left[\frac{6x}{\pi} \right] \cos \left[\frac{3x}{\pi} \right],$
 where $[y]$ denotes the largest integer less than or equal to y
- (C) Volume of the parallelopiped with its edges represented by the vectors
 $\hat{i} + \hat{j}, \hat{i} + 2\hat{j}$ and $\hat{i} + \hat{j} + \pi\hat{k}$
- (D) Angle between vectors \vec{a} and \vec{b} where \vec{a}, \vec{b} and \vec{c} are unit vectors satisfying
 $\vec{a} + \vec{b} + \sqrt{3}\vec{c} = \vec{0}$

Column II

- (p) $\frac{\pi}{6}$
- (q) $\frac{\pi}{4}$
- (r) $\frac{\pi}{3}$
- (s) $\frac{\pi}{2}$
- (t) π

Answer

	p	q	r	s	t
A	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>
B	<input checked="" type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>
C	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>
D	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>

30. Match the statements/expressions given in **Column I** with the values given in **Column II**.

Column I

- (A) The number of solutions of the equation
 $x e^{\sin x} - \cos x = 0$
 in the interval $\left(0, \frac{\pi}{2}\right)$
- (B) Value(s) of k for which the planes
 $kx + 4y + z = 0$, $4x + ky + 2z = 0$ and $2x + 2y + z = 0$
 intersect in a straight line
- (C) Value(s) of k for which
 $|x-1| + |x-2| + |x+1| + |x+2| = 4k$
 has integer solution(s)
- (D) If
 $y' = y + 1$ and $y(0) = 1$,
 then value(s) of $y(\ln 2)$

Column II

- (p) 1
 (q) 2
 (r) 3
 (s) 4
 (t) 5

Answer

	p	q	r	s	t
A	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
B	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>
C	<input type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>
D	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>

SECTION - IV**Integer Answer Type**

This section contains 8 questions. The answer to each of the questions is a single-digit integer, ranging from 0 to 9. The appropriate bubbles below the respective question numbers in the ORS have to be darkened. For example, if the correct answers to question numbers X, Y, Z and W (say) are 6, 0, 9 and 2, respectively, then the correct darkening of bubbles will look like the following:

X	Y	Z	W
<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>
<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>
<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>

31. The maximum value of the function $f(x) = 2x^3 - 15x^2 + 36x - 48$ on the set
 $A = \{x \mid x^2 + 20 \leq 9x\}$ is

Answer

<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>
0	1	2	3	4	5	6	7	8

32. Let (x, y, z) be points with integer coordinates satisfying the system of homogeneous equations:

$$\begin{aligned} 3x - y - z &= 0 \\ -3x + z &= 0 \\ -3x + 2y + z &= 0. \end{aligned}$$

Then the number of such points for which $x^2 + y^2 + z^2 \leq 100$ is

Answer

- (0) (1) (2) (3) (4) (5) (6) (7) (8) (9)

33. Let ABC and ABC' be two non-congruent triangles with sides $AB = 4$, $AC = AC' = 2\sqrt{2}$ and angle $B = 30^\circ$. The absolute value of the difference between the areas of these triangles is

Answer

- (0) (1) (2) (3) (4) (5) (6) (7) (8) (9)

34. Let $p(x)$ be a polynomial of degree 4 having extremum at $x = 1, 2$ and

$$\lim_{x \rightarrow 0} \left(1 + \frac{p(x)}{x^2} \right) = 2.$$

Then the value of $p(2)$ is

Answer

- (0) (1) (2) (3) (4) (5) (6) (7) (8) (9)

35. Let $f: \mathbf{R} \rightarrow \mathbf{R}$ be a continuous function which satisfies

$$f(x) = \int_0^x f(t) dt.$$

Then the value of $f(\ln 5)$ is

Answer

- (0) (1) (2) (3) (4) (5) (6) (7) (8) (9)

36. The centres of two circles C_1 and C_2 each of unit radius are at a distance of 6 units from each other. Let P be the mid point of the line segment joining the centres of C_1 and C_2 and C be a circle touching circles C_1 and C_2 externally. If a common tangent to C_1 and C passing through P is also a common tangent to C_2 and C , then the radius of the circle C is

Answer

- (0) (1) (2) (3) (4) (5) (6) (7) (8) (9)

37. The smallest value of k , for which both the roots of the equation

$$x^2 - 8kx + 16(k^2 - k + 1) = 0$$

are real, distinct and have values at least 4, is

Answer

- (0) (1) (2) (3) (4) (5) (6) (7) (8) (9)

38. If the function $f(x) = x^3 + e^{\frac{x}{2}}$ and $g(x) = f^{-1}(x)$, then the value of $g'(1)$ is

Answer

- (0) (1) (2) (3) (4) (5) (6) (7) (8) (9)

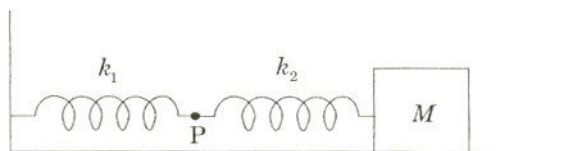
PART III : PHYSICS

SECTION - I

Single Correct Choice Type

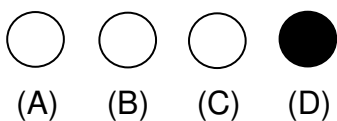
This section contains 4 multiple choice questions. Each question has 4 choices (A), (B), (C) and (D) for its answer, out of which **ONLY ONE** is correct.

39. The mass M shown in the figure oscillates in simple harmonic motion with amplitude A . The amplitude of the point P is



- (A) $\frac{k_1 A}{k_2}$ (B) $\frac{k_2 A}{k_1}$ (C) $\frac{k_1 A}{k_1 + k_2}$ (D) $\frac{k_2 A}{k_1 + k_2}$

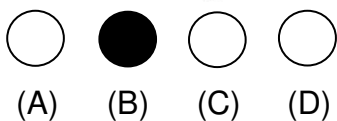
Answer



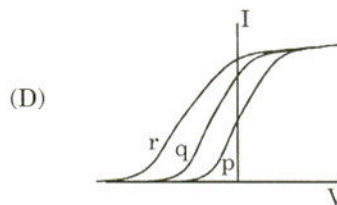
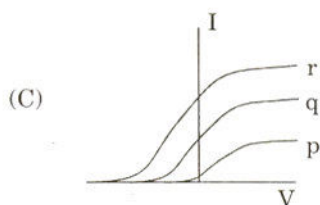
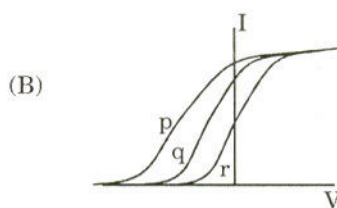
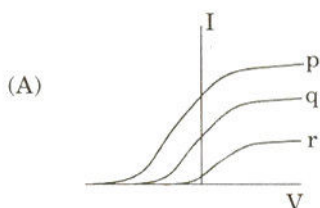
40. A piece of wire is bent in the shape of a parabola $y = kx^2$ (y -axis vertical) with a bead of mass m on it. The bead can slide on the wire without friction. It stays at the lowest point of the parabola when the wire is at rest. The wire is now accelerated parallel to the x -axis with a constant acceleration a . The distance of the new equilibrium position of the bead, where the bead can stay at rest with respect to the wire, from the y -axis is

- (A) $\frac{a}{gk}$ (B) $\frac{a}{2gk}$ (C) $\frac{2a}{gk}$ (D) $\frac{a}{4gk}$

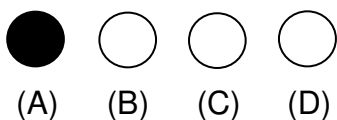
Answer



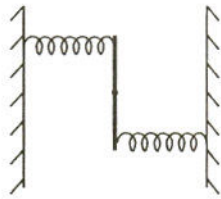
41. Photoelectric effect experiments are performed using three different metal plates p, q and r having work functions $\phi_p = 2.0$ eV, $\phi_q = 2.5$ eV and $\phi_r = 3.0$ eV, respectively. A light beam containing wavelengths of 550 nm, 450 nm and 350 nm with equal intensities illuminates each of the plates. The correct I-V graph for the experiment is [Take $hc = 1240$ eV nm]



Answer



42. A uniform rod of length L and mass M is pivoted at the centre. Its two ends are attached to two springs of equal spring constants k . The springs are fixed to rigid supports as shown in the figure, and the rod is free to oscillate in the horizontal plane. The rod is gently pushed through a small angle θ in one direction and released. The frequency of oscillation is



- (A) $\frac{1}{2\pi} \sqrt{\frac{2k}{M}}$ (B) $\frac{1}{2\pi} \sqrt{\frac{k}{M}}$ (C) $\frac{1}{2\pi} \sqrt{\frac{6k}{M}}$ (D) $\frac{1}{2\pi} \sqrt{\frac{24k}{M}}$

Answer



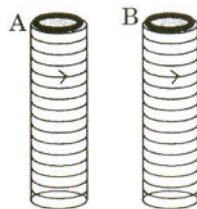
(A) (B) (C) (D)

SECTION - II

Multiple Correct Choice Type

This section contains 5 multiple choice questions. Each question has 4 choices (A), (B), (C) and (D) for its answer, out of which **ONE OR MORE** is/are correct.

43. Two metallic rings A and B, identical in shape and size but having different resistivities ρ_A and ρ_B , are kept on top of two identical solenoids as shown in the figure. When current I is switched on in both the solenoids in identical manner, the rings A and B jump to heights h_A and h_B , respectively, with $h_A > h_B$. The possible relation(s) between their resistivities and their masses m_A and m_B is(are)



- (A) $\rho_A > \rho_B$ and $m_A = m_B$ (B) $\rho_A < \rho_B$ and $m_A = m_B$
(C) $\rho_A > \rho_B$ and $m_A > m_B$ (D) $\rho_A < \rho_B$ and $m_A < m_B$

Answer



(A) (B) (C) (D)

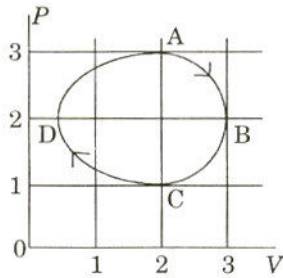
44. A student performed the experiment to measure the speed of sound in air using resonance air-column method. Two resonances in the air-column were obtained by lowering the water level. The resonance with the shorter air-column is the first resonance and that with the longer air-column is the second resonance. Then,
- (A) the intensity of the sound heard at the first resonance was more than that at the second resonance
- (B) the prongs of the tuning fork were kept in a horizontal plane above the resonance tube
- (C) the amplitude of vibration of the ends of the prongs is typically around 1 cm
- (D) the length of the air-column at the first resonance was somewhat shorter than $1/4$ th of the wavelength of the sound in air

Answer



(A) (B) (C) (D)

45. The figure shows the P - V plot of an ideal gas taken through a cycle ABCDA. The part ABC is a semi-circle and CDA is half of an ellipse. Then,



- (A) the process during the path $A \rightarrow B$ is isothermal
 (B) heat flows out of the gas during the path $B \rightarrow C \rightarrow D$
 (C) work done during the path $A \rightarrow B \rightarrow C$ is zero
 (D) positive work is done by the gas in the cycle ABCDA

Answer

- ☐ (A) ☒ (B) ☐ (C) ☒ (D)

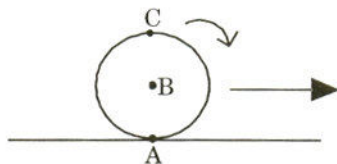
46. Under the influence of the Coulomb field of charge $+Q$, a charge $-q$ is moving around it in an elliptical orbit. Find out the correct statement(s).

- (A) The angular momentum of the charge $-q$ is constant
 (B) The linear momentum of the charge $-q$ is constant
 (C) The angular velocity of the charge $-q$ is constant
 (D) The linear speed of the charge $-q$ is constant

Answer

- ☒ (A) ☐ (B) ☐ (C) ☐ (D)

47. A sphere is rolling without slipping on a fixed horizontal plane surface. In the figure, A is the point of contact, B is the centre of the sphere and C is its topmost point. Then,



- (A) $\vec{V}_C - \vec{V}_A = 2(\vec{V}_B - \vec{V}_C)$ (B) $\vec{V}_C - \vec{V}_B = \vec{V}_B - \vec{V}_A$
 (C) $|\vec{V}_C - \vec{V}_A| = 2|\vec{V}_B - \vec{V}_C|$ (D) $|\vec{V}_C - \vec{V}_A| = 4|\vec{V}_B|$

Answer

- ☐ (A) ☒ (B) ☒ (C) ☐ (D)

SECTION – III

Matrix – Match Type

This section contains 2 questions. Each question contains statements given in two columns, which have to be matched. The statements in **Column I** are labelled A, B, C and D, while the statements in **Column II** are labelled p, q, r, s and t. Any given statement in **Column I** can have correct matching with **ONE OR MORE** statement(s) in **Column II**. The appropriate bubbles corresponding to the answers to these questions have to be darkened as illustrated in the following example:

If the correct matches are A – p, s and t; B – q and r; C – p and q; and D – s and t; then the correct darkening of bubbles will look like the following.

	p	q	r	s	t
A	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>
B	<input type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>
C	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
D	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>

48. **Column II** gives certain systems undergoing a process. **Column I** suggests changes in some of the parameters related to the system. Match the statements in **Column I** to the appropriate process(es) from **Column II**.

Column I

- (A) The energy of the system is increased
- (B) Mechanical energy is provided to the system, which is converted into energy of random motion of its parts
- (C) Internal energy of the system is converted into its mechanical energy
- (D) Mass of the system is decreased

Column II

- (p) System: A capacitor, initially uncharged
Process: It is connected to a battery
- (q) System: A gas in an adiabatic container fitted with an adiabatic piston
Process: The gas is compressed by pushing the piston
- (r) System: A gas in a rigid container
Process: The gas gets cooled due to colder atmosphere surrounding it
- (s) System: A heavy nucleus, initially at rest
Process: The nucleus fissions into two fragments of nearly equal masses and some neutrons are emitted
- (t) System: A resistive wire loop
Process: The loop is placed in a time varying magnetic field perpendicular to its plane

Answer

	p	q	r	s	t
A	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>
B	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
C	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>
D	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>

49. **Column I** shows four situations of standard Young's double slit arrangement with the screen placed far away from the slits S_1 and S_2 . In each of these cases $S_1P_0 = S_2P_0$, $S_1P_1 - S_2P_1 = \lambda/4$ and $S_1P_2 - S_2P_2 = \lambda/3$, where λ is the wavelength of the light used. In the cases B, C and D, a transparent sheet of refractive index μ and thickness t is pasted on slit S_2 . The thicknesses of the sheets are different in different cases. The phase difference between the light waves reaching a point P on the screen from the two slits is denoted by $\delta(P)$ and the intensity by $I(P)$. Match each situation given in **Column I** with the statement(s) in **Column II** valid for that situation.

	Column I	Column II
(A)		(p) $\delta(P_0) = 0$
(B)	$(\mu - 1)t = \lambda/4$	(q) $\delta(P_1) = 0$
(C)	$(\mu - 1)t = \lambda/2$	(r) $I(P_1) = 0$
(D)	$(\mu - 1)t = 3\lambda/4$	(s) $I(P_0) > I(P_1)$
		(t) $I(P_2) > I(P_1)$

Answer

	p	q	r	s	t
A	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>
B	<input type="radio"/>	<input checked="" type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>
C	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>
D	<input type="radio"/>	<input type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>	<input checked="" type="radio"/>

Integer Answer Type

This section contains 8 questions. The answer to each of the questions is a single-digit integer, ranging from 0 to 9. The appropriate bubbles below the respective question numbers in the ORS have to be darkened. For example, if the correct answers to question numbers X, Y, Z and W (say) are 6, 0, 9 and 2, respectively, then the correct darkening of bubbles will look like the following:

X	Y	Z	W
0	0	0	0
1	1	1	1
2	2	2	2
3	3	3	3
4	4	4	4
5	5	5	5
6	6	6	6
7	7	7	7
8	8	8	8
9	9	9	9

50. A metal rod AB of length $10x$ has its one end A in ice at 0°C and the other end B in water at 100°C . If a point P on the rod is maintained at 400°C , then it is found that equal amounts of water and ice evaporate and melt per unit time. The latent heat of evaporation of water is 540 cal/g and latent heat of melting of ice is 80 cal/g . If the point P is at a distance of λx from the ice end A, find the value of λ .
[Neglect any heat loss to the surrounding.]

Answer

0 1 2 3 4 5 6 7 8 9

51. A cylindrical vessel of height 500 mm has an orifice (small hole) at its bottom. The orifice is initially closed and water is filled in it up to height H. Now the top is completely sealed with a cap and the orifice at the bottom is opened. Some water comes out from the orifice and the water level in the vessel becomes steady with height of water column being 200 mm. Find the fall in height (in mm) of water level due to opening of the orifice.
[Take atmospheric pressure $= 1.0 \times 10^5 \text{ N/m}^2$, density of water $= 1000 \text{ kg/m}^3$ and $g = 10 \text{ m/s}^2$. Neglect any effect of surface tension.]

Answer

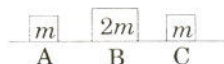
0 1 2 3 4 5 6 7 8 9

52. Two soap bubbles A and B are kept in a closed chamber where the air is maintained at pressure 8 N/m^2 . The radii of bubbles A and B are 2 cm and 4 cm, respectively. Surface tension of the soap-water used to make bubbles is 0.04 N/m . Find the ratio n_B/n_A , where n_A and n_B are the number of moles of air in bubbles A and B, respectively. [Neglect the effect of gravity.]

Answer

0 1 2 3 4 5 6 7 8 9

53. Three objects A, B and C are kept in a straight line on a frictionless horizontal surface. These have masses m , $2m$ and m , respectively. The object A moves towards B with a speed 9 m/s and makes an elastic collision with it. Thereafter, B makes completely inelastic collision with C. All motions occur on the same straight line. Find the final speed (in m/s) of the object C.



Answer

0 1 2 3 4 5 6 7 8 9

54. A steady current I goes through a wire loop PQR having shape of a right angle triangle with $PQ = 3x$, $PR = 4x$ and $QR = 5x$. If the magnitude of the magnetic field at P due to this loop is $k \left(\frac{\mu_0 I}{48\pi x} \right)$, find the value of k .

Answer

☐ 0 ☐ 1 ☐ 2 ☐ 3 ☐ 4 ☐ 5 ☐ 6 ☒ 7 ☐ 8 ☐ 9

55. A light inextensible string that goes over a smooth fixed pulley as shown in the figure connects two blocks of masses 0.36 kg and 0.72 kg. Taking $g = 10 \text{ m/s}^2$, find the work done (in joules) by the string on the block of mass 0.36 kg during the first second after the system is released from rest.



Answer

☐ 0 ☐ 1 ☐ 2 ☐ 3 ☐ 4 ☐ 5 ☐ 6 ☐ 7 ☒ 8 ☐ 9

56. A solid sphere of radius R has a charge Q distributed in its volume with a charge density $\rho = \kappa r^a$, where κ and a are constants and r is the distance from its centre. If the electric field at $r = \frac{R}{2}$ is $\frac{1}{8}$ times that at $r = R$, find the value of a .

Answer

☐ 0 ☐ 1 ☒ 2 ☐ 3 ☐ 4 ☐ 5 ☐ 6 ☐ 7 ☐ 8 ☐ 9

57. A 20 cm long string, having a mass of 1.0 g, is fixed at both the ends. The tension in the string is 0.5 N. The string is set into vibrations using an external vibrator of frequency 100 Hz. Find the separation (in cm) between the successive nodes on the string.

Answer

☐ 0 ☐ 1 ☐ 2 ☐ 3 ☐ 4 ☒ 5 ☐ 6 ☐ 7 ☐ 8 ☐ 9